

# Demand Slides

**Econ 360**

Summer 2025



# Learning Outcomes/Goals

- 1 Algebraically and graphically if a good is ordinary versus Giffen, and normal versus inferior from a consumer's utility function.
- 2 Algebraically and graphically determine if two goods are substitutes, complements, or neither.
- 3 Understand where the demand curves you see in other classes ultimately come from!

# Where We Are/Going

- ◇ We **know** how to find a consumer's optimal bundle.
  - ▶ Where the optimal bundle is based on prices of the commodities and the consumer's income, wealth, or amount of money they have to spend.
- ◇ A demand curve from intro micro shows quantity demanded for **any** price.
  - ▶ How can we use what we know to make a demand curve for any consumer?

# A consumer's demand

- ◇ Consider a Cobb-Douglass utility function  $U = x^\alpha y^\beta$  with budget  $p_x x + p_y y \leq m$ .
- ◇ **Review:** We know optimal bundles!
  - ▶  $x^* = \frac{\alpha}{\alpha+\beta} \cdot \frac{m}{p_x}$ .
  - ▶  $y^* = \frac{\beta}{\alpha+\beta} \cdot \frac{m}{p_y}$ .
- ◇ So if we increase the price of either  $x$ , and keep price of  $y$  the same, then the amount of  $x$  the consumer buys at the optimum goes down!
- ◇ And therefore, the consumer's demand for  $x$  decreases as the price increases, just like a classical demand curve you have seen before.

# A consumer's demand

- ◇ Consider a Cobb-Douglas utility function  $U = x^\alpha y^\beta$  with budget  $p_x x + p_y y \leq m$ .

- ▶  $x^* = \frac{\alpha}{\alpha+\beta} \cdot \frac{m}{p_x}$ .

- ▶  $y^* = \frac{\beta}{\alpha+\beta} \cdot \frac{m}{p_y}$ .

- ◇ As income increases,  $m \uparrow$  and consumer demand increases as income increases.
- ◇ Let's add some formal econ vocabulary to these concepts!

# The 4 Types of Goods

		Income ↑	
		Demand ↑	Demand ↓
Price of X ↑	Demand ↑	Giffen, Normal	Giffen, Inferior
	Demand ↓	Ordinary, Normal	Ordinary, Inferior

- ◇ **Note:** How we characterize a good based on price changes is **unrelated/independent of** how we characterize a good based on income changes!

# Substitutes, Complements, or Neither

## ◇ **Substitutes**

- ▶ We know perfect substitutes are when a consumer is always willing to trade between two goods at a fixed ratio.
- ▶ But what about when a consumer is willing to trade between goods, just at a non-fixed, or variable, rate?
- ▶ For example, Dr.Pepper and Ginger-Ale.

## ◇ **Complements**

- ▶ We know perfect complements are when a consumer always consumes two goods in a fixed ratio.
- ▶ But what about when a consumer likes consuming both goods together, just not in a fixed ratio?
- ▶ For example: peanut butter and jelly.

- ◇ **Question:** How can we use our demand function to tell if two goods are complements or substitutes?

# Demand and Substitutes

- ◇ Consider the following demand equations for two goods  $x$  and  $y$  with prices  $p_x, p_y$  and income  $m$ .
  - ▶  $x^* = m \cdot p_y$ .
  - ▶  $y^* = m \cdot p_x$ .
- ◇ For each good, when the price of the other good increases demand increases.
  - ▶ For example,  $\frac{\partial x^*}{\partial p_y} = m > 0$ , so  $x$  and  $y$  are substitutes!



# Demand and Complements

- ◇ Consider the following demand equations for two goods  $x$  and  $y$  with prices  $p_x, p_y$  and income  $m$ .
  - ▶  $x^* = \frac{m}{p_y}$ .
  - ▶  $y^* = \frac{m}{p_x}$ .
- ◇ For each good, when the price of the other good increases demand decreases.
  - ▶ For example,  $\frac{\partial x^*}{\partial p_y} = \frac{-m}{p_y^2} < 0$ , so  $x$  and  $y$  are complements!

# Back to our example

- ◇ Consider a Cobb-Douglas utility function  $U = x^\alpha y^\beta$  with budget  $p_x x + p_y y \leq m$ .
  - ▶  $x^* = \frac{\alpha}{\alpha+\beta} \cdot \frac{m}{p_x}$ .
  - ▶  $y^* = \frac{\beta}{\alpha+\beta} \cdot \frac{m}{p_y}$ .
- ◇ Question: How would you characterize these two goods?  
Normal vs Inferior, Ordinary vs Giffen?
- ◇ Are these two goods substitutes, complements, or neither?

# Characterizing Goods

- ◇ Consider a Cobb-Douglass utility function  $U = x^\alpha y^\beta$  with budget  $p_x x + p_y y \leq m$ .

- ▶  $x^* = \frac{\alpha}{\alpha+\beta} \cdot \frac{m}{p_x}$ .

- ▶  $y^* = \frac{\beta}{\alpha+\beta} \cdot \frac{m}{p_y}$ .

- ◇ **Normal or Inferior?**

- ▶  $\frac{\partial x^*}{\partial m} = \frac{\alpha}{\alpha+\beta} \cdot \frac{1}{p_x}$ .

- ▶  $\frac{\partial y^*}{\partial m} = \frac{\beta}{\alpha+\beta} \cdot \frac{1}{p_y}$ .

- ▶ These are both positive, so  $x$  and  $y$  are **Normal**.

- ◇ **Ordinary or Giffen?**

- ▶  $\frac{\partial x^*}{\partial p_x} = \frac{\alpha}{\alpha+\beta} \cdot \frac{-m}{p_x^2}$ .

- ▶  $\frac{\partial y^*}{\partial p_y} = \frac{\beta}{\alpha+\beta} \cdot \frac{-m}{p_y^2}$ .

- ▶ These are both negative, so  $x$  and  $y$  are **Ordinary**.

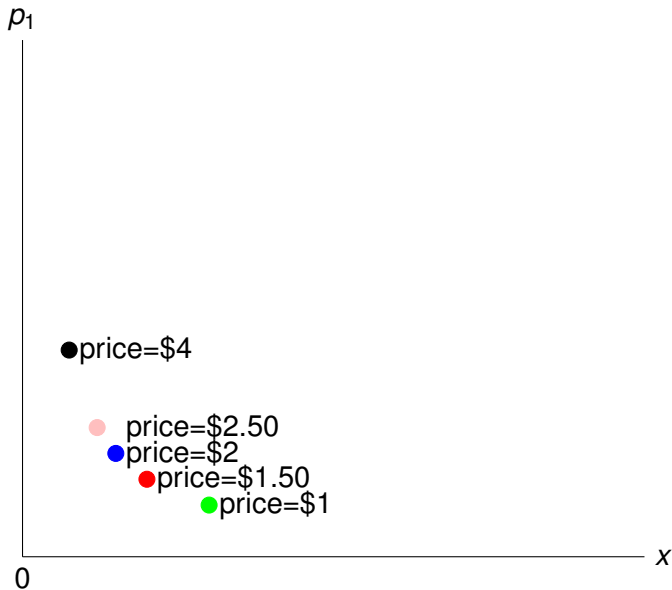
# Substitutes or Complements?

- ◇ Consider a Cobb-Douglas utility function  $U = x^\alpha y^\beta$  with budget  $p_x x + p_y y \leq m$ .
  - ▶  $x^* = \frac{\alpha}{\alpha+\beta} \cdot \frac{m}{p_x}$ .
  - ▶  $y^* = \frac{\beta}{\alpha+\beta} \cdot \frac{m}{p_y}$ .
- ◇ **Substitutes, Complements, or Neither?**
  - ▶  $\frac{\partial x^*}{\partial p_y} = 0$ .
  - ▶  $\frac{\partial y^*}{\partial p_x} = 0$ .
  - ▶ These are both 0, so the two goods are neither substitutes nor complements.

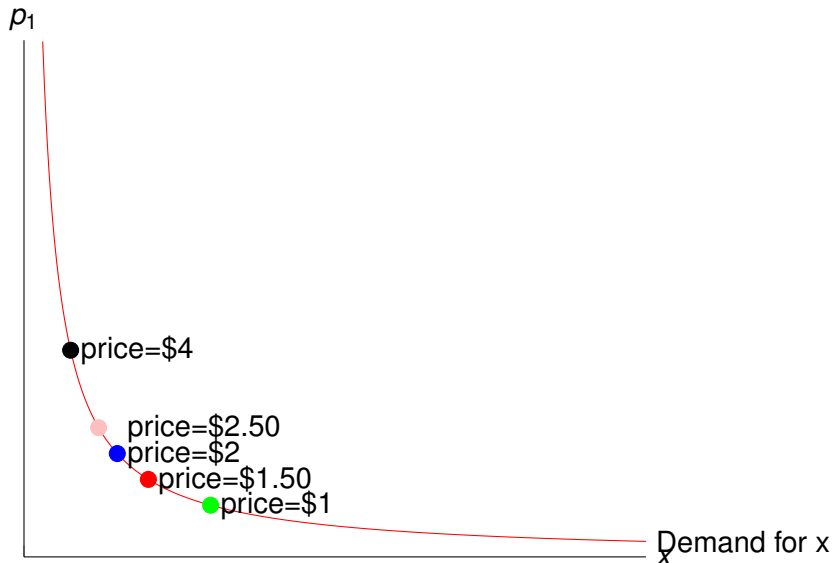
# Creating a Demand Curve for X

- ◇ What is a demand curve?
- ◇ It is a relationship between price and quantity demanded, holding constant all other prices and income.
- ◇ Let's use our demand for x:  $x^* = \frac{\alpha}{\alpha + \beta} \cdot \frac{m}{p_x}$ .
  - ▶ We will hold constant  $m$  and  $p_y$ . Let's plug in a bunch of different prices and plot this!
  - ▶ Suppose  $\alpha = \beta = 1$  and  $m = 6$ .

# Creating a Demand Curve for X



# Creating a Demand Curve for X

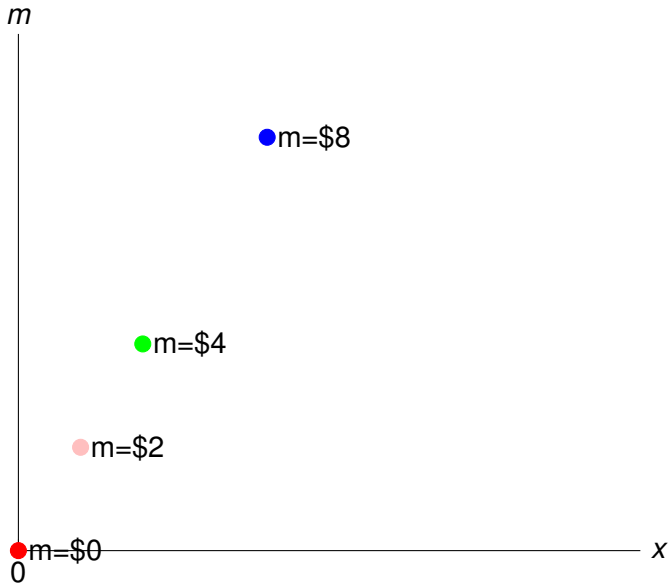


# What about Demand vs Income?

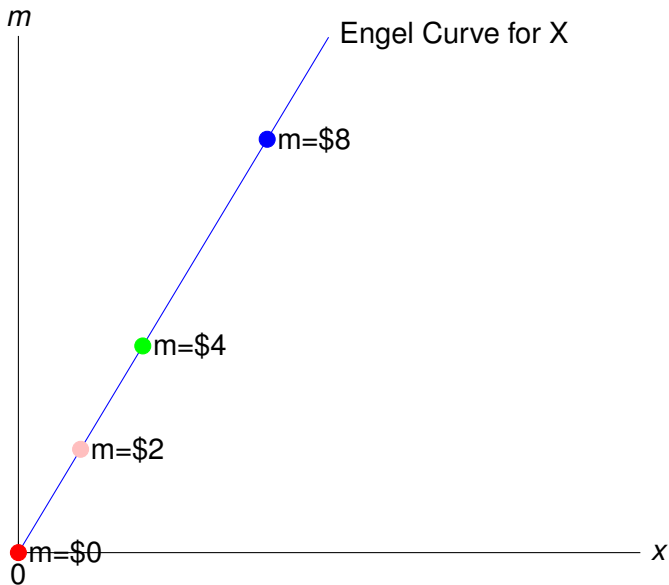
- ◇ We can create a similar graph showing demand for  $x$  holding constant  $p_x$ ,  $p_y$ , and changing  $m$ .
- ◇ We call that an Engel curve.
- ◇ Let's again use our demand for  $x$ :  $x^* = \frac{\alpha}{\alpha+\beta} \cdot \frac{m}{p_x}$ .
- ◇ Suppose  $\alpha = \beta = 1$  and  $p_x = p_y = 1$ .
- ◇ So  $x_1 = \frac{1}{2} \cdot m$ .



# Engel Curve



# Engel Curve



# Wealth Expansion Curve and Price Offer Curve

- ◇ Demand curves and Engel curves show a single good.
- ◇ What if we want to show both goods on one graph when  
i) income changes and ii) the price of only one good changes?
  - ▶ i) Wealth Expansion
  - ▶ ii) Price Offer Curve

# Big Question for Class

How can we use our utility maximization diagram to trace out a demand curve and an Engel curve for good  $x$ ?

- ◇ In 160, you found elasticities as the percentage change in quantity demanded for a 1% change in price, or  $\frac{\Delta Q^d}{\Delta P}$ .
- ◇ Our  $Q^d$  is just the demand for each good, and we have the price in the demand function.
- ◇ So we can use the derivative of demand to not only say whether a good is ordinary or Giffen, but also a consumer's elasticity of demand!
- ◇ This will come back later in the semester and when we talk about aggregate demand/supply!